## Exercise 50

Suppose that a function $f$ is continuous on $[0,1]$ except at 0.25 and that $f(0)=1$ and $f(1)=3$. Let $N=2$. Sketch two possible graphs of $f$, one showing that $f$ might not satisfy the conclusion of the Intermediate Value Theorem and one showing that $f$ might still satisfy the conclusion of the Intermediate Value Theorem (even though it doesn't satisfy the hypothesis).

## Solution

The graph of the function below shows how if there's a discontinuity, not all $y$-values between 1 and 3 can be covered.


The graph of the function below shows how if there's a discontinuity, all $y$-values between 1 and 3 can be covered.


